

Parallel Anisotropic Unstructured Grid Adaptation

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Michael A. Park

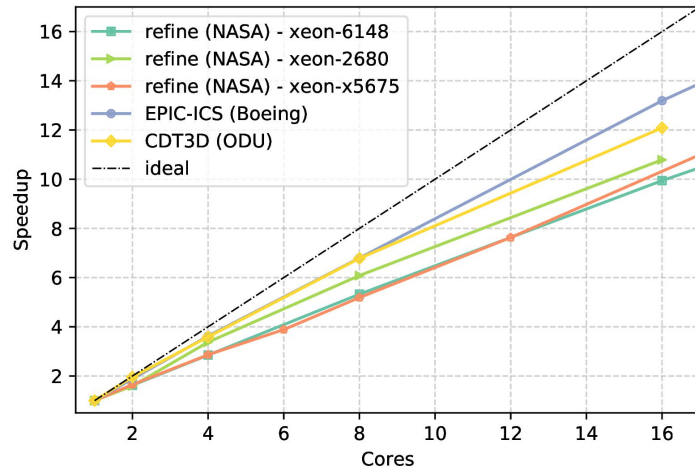
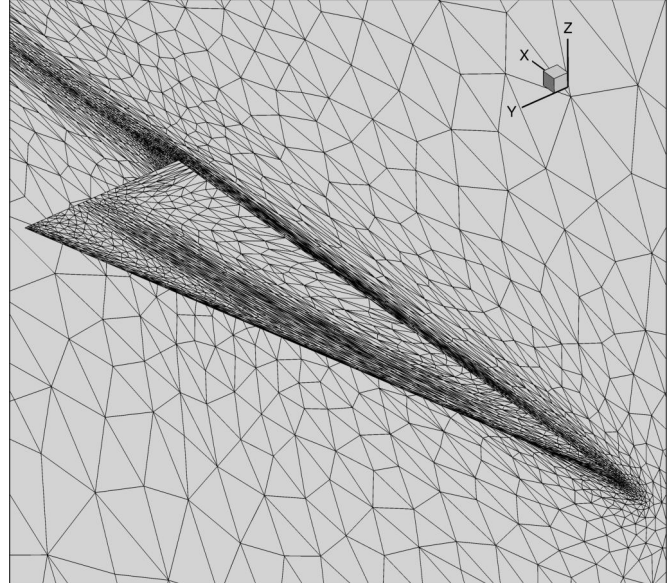
NASA Langley Research Center, Hampton, VA

Adrien Loseille

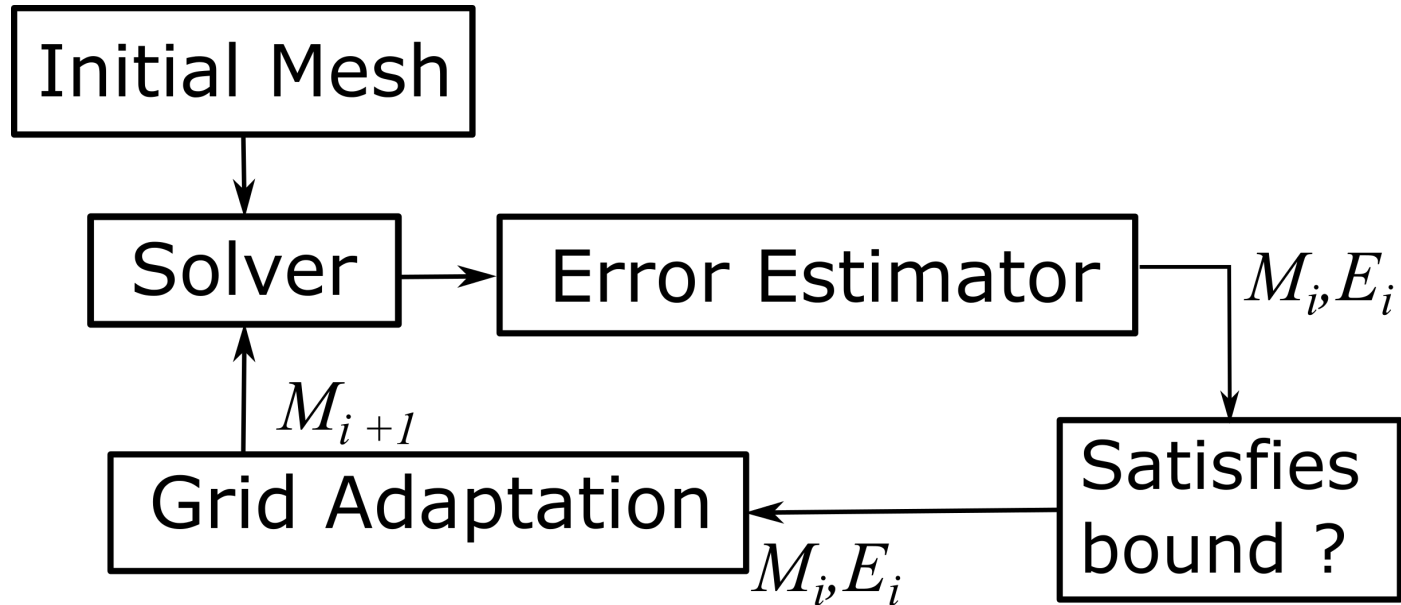
INRIA Paris-Saclay, France

Todd Michal

The Boeing Company, St. Louis, MO

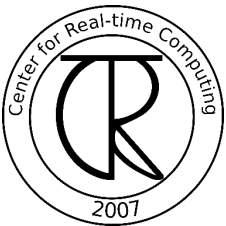


Grid adaptation as part of the CFD pipeline



Grid Adaptation

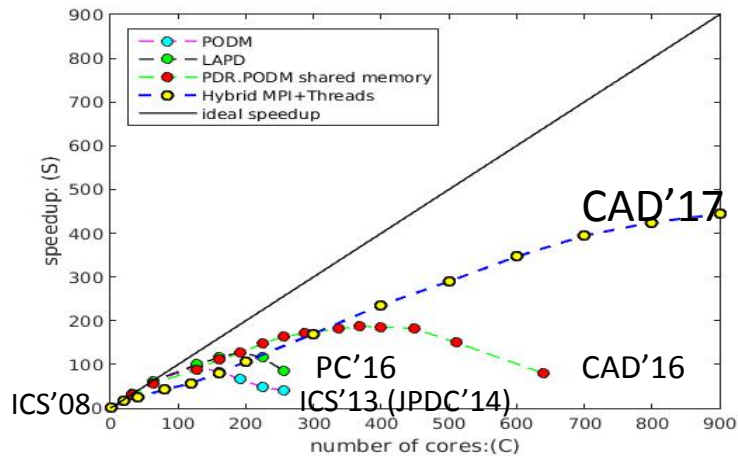
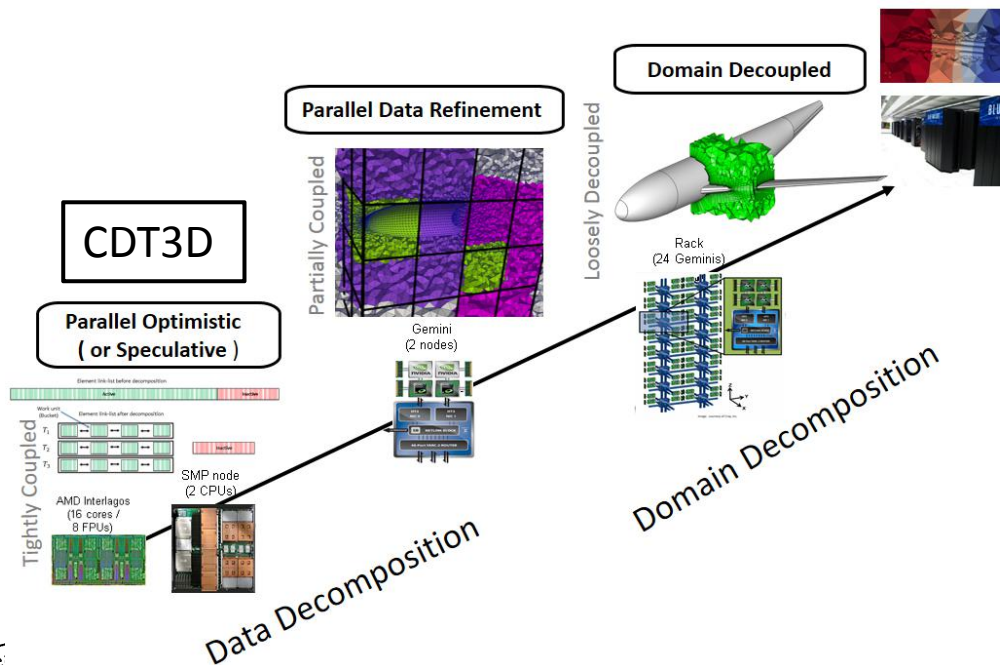
- Anisotropic Metric
 - Supplies grid adaptation software with a metric tensor (3x3) that encapsulates desired size and direction
 - Analytic Metric
 - Easily evaluated function that models a curved flow shear layer
 - Multiscale
 - Recovered Mach Hessian, scaled to control L2 norm of interpolation error at specified complexity (adapted grid size)
 - Theory [1] and experiments [2] show second-order interpolation error control



[1] A. Loseille and F. Alauzet, "Continuous Mesh Framework Part I: Well-Posed Continuous Interpolation Error," SIAM J. Numer. Anal., vol. 49, no. 1, pp. 38–60, Jan. 2011.

[2] A. Loseille, A. Dervieux, P. Frey, and F. Alauzet, "Achievement of Global Second Order Mesh Convergence for Discontinuous Flows with Adapted Unstructured Meshes," AIAA 2007-4186

Telescopic Approach for Grid Generation & Adaptation

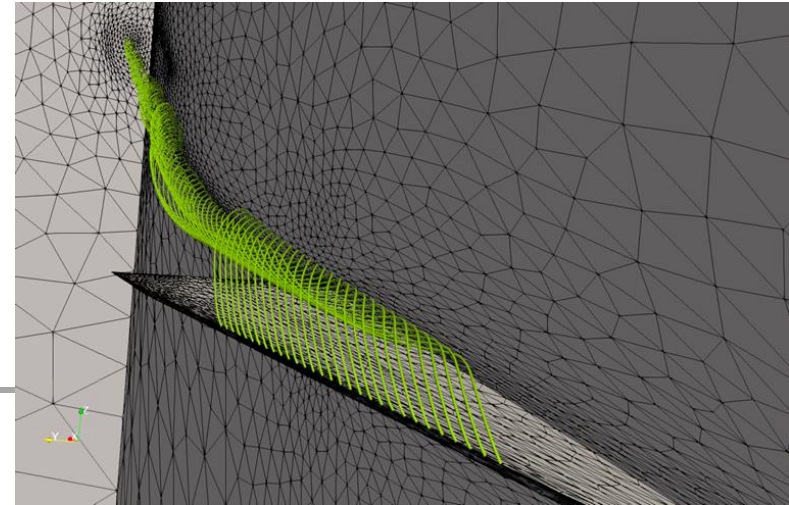
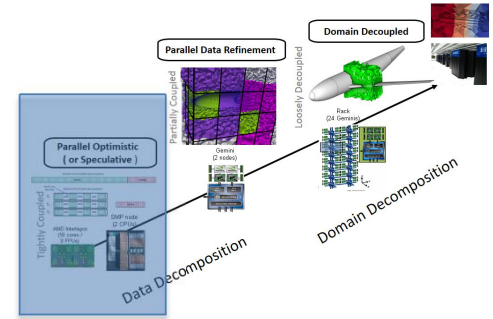


Telescopic Approach for Extreme-scale Parallel Mesh Generation for CFD Applications. Nikos Chrisochoides Published in AIAA Aviation Forum, Washington DC, June, 2016.

Methods (scalability-first)

CDT3D

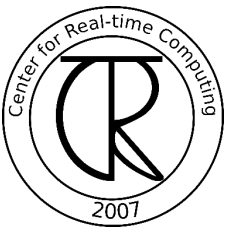
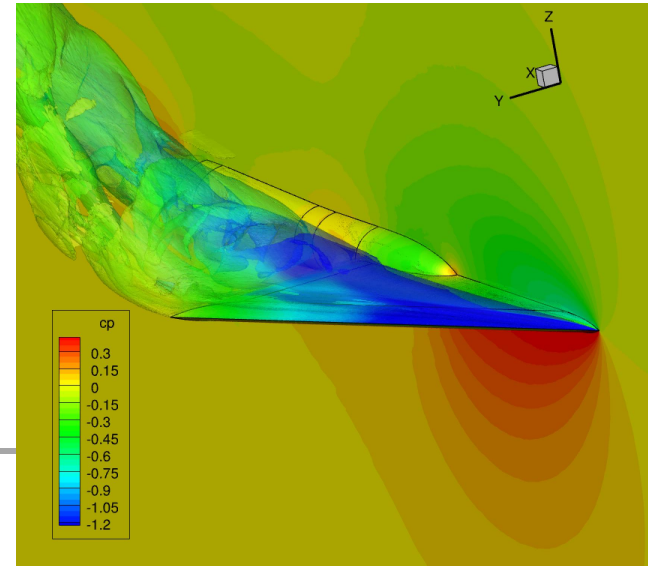
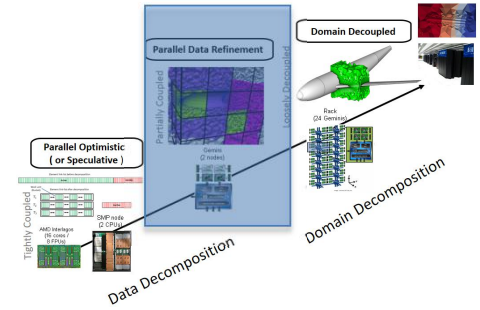
- CRTC, Old Dominion University
- Data Decomposition
- Fine-grained scheme for local reconnection
- Speculative execution



Methods (scalability-first)

refine

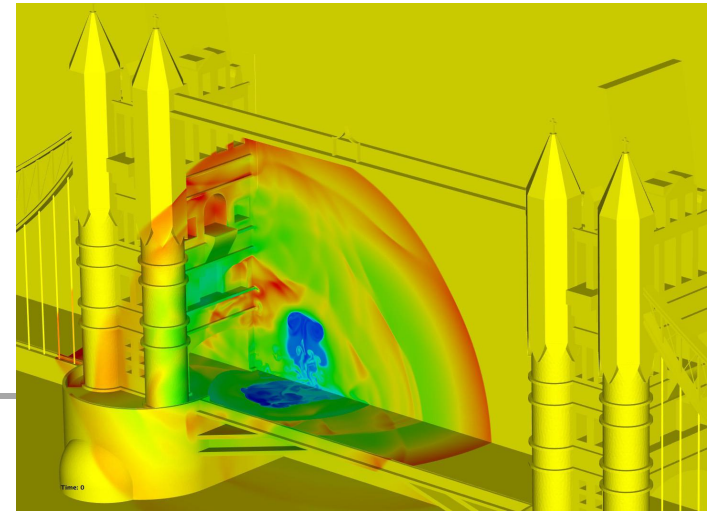
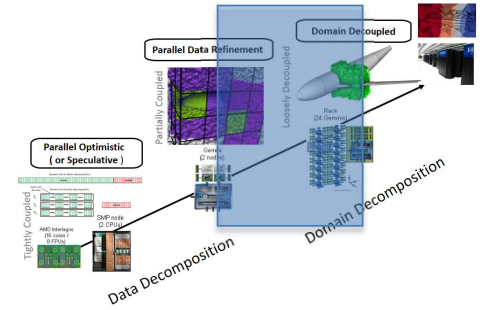
- NASA/LaRC
- Domain decomposition (ParMetis/Zoltan)
- Local grid operators of element split, element collapse, and node movement
- Homogeneous programming model
- Message Passing



Methods (functionality-first)

Feflo.a

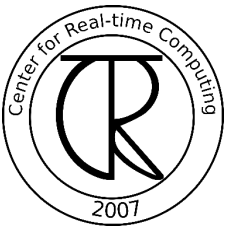
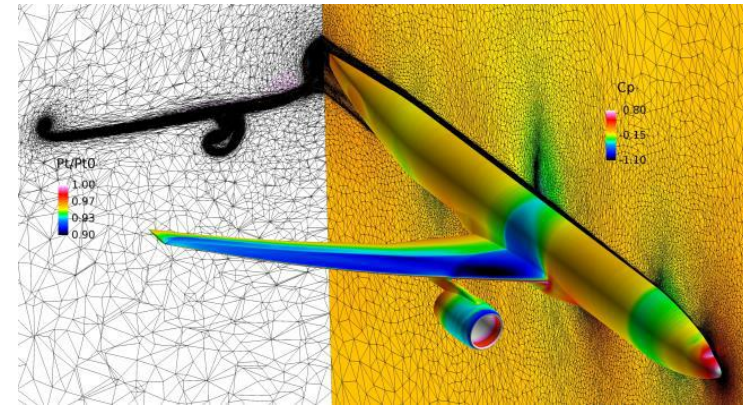
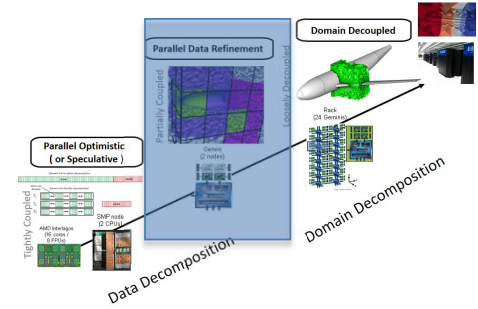
- INRIA
- Hierarchical Domain Decomposition
- Cavity operator
- Unix pipes



Methods (functionality-first)

EPIC

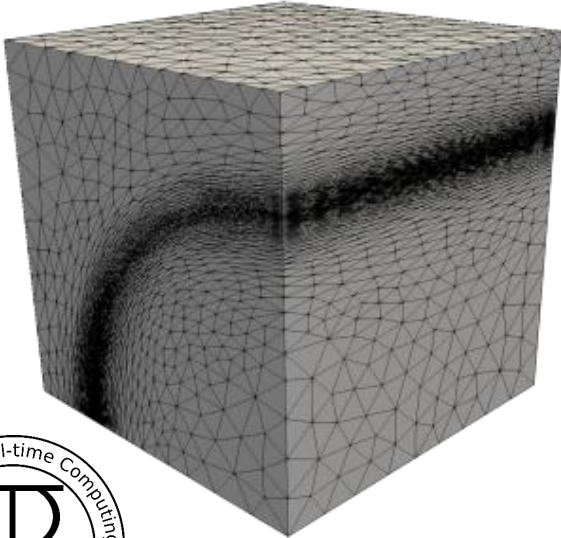
- The Boeing Company
- Coarse-grain parallelism at subdomain level
- Refinement, coarsening, reconnection and smoothing
- Message Passing



Test Cases

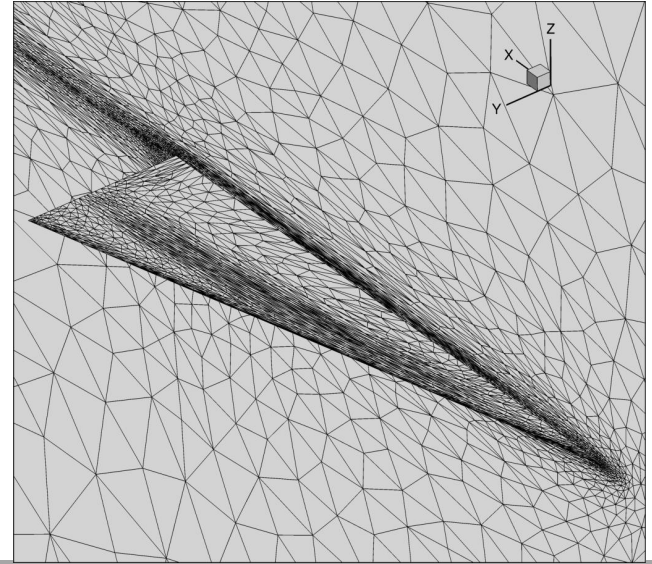
Metric tensor field :

- Analytic Metric
- Target Complexity 500k



Metric tensor field :

- Multiscale metric based on the Mach field
- Target Complexities 500k, 10M



Evaluation Criteria

- Scalability

- Parallel execution time versus using sequential execution

- Quality

- Edge Length (in metric space)

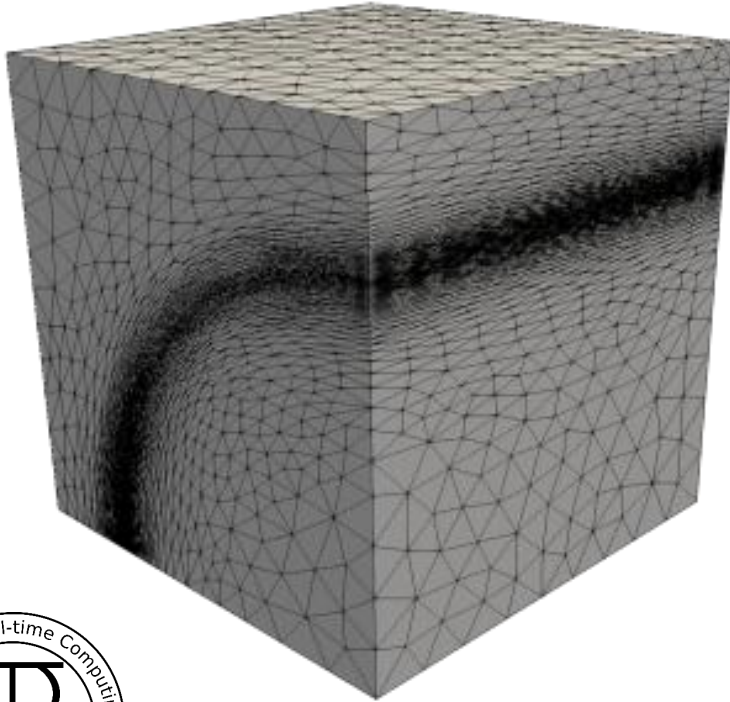
$$\text{length}(a, b) = \frac{\ell_a - \ell_b}{\log(\ell_a) - \log(\ell_b)}$$

- Mean ratio (in metric space)

$$\text{quality}(K) = f \left(\frac{\text{volume}^{2/3}}{\sqrt{\sum(\text{edge.length})^2}} \right)$$



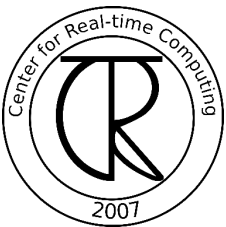
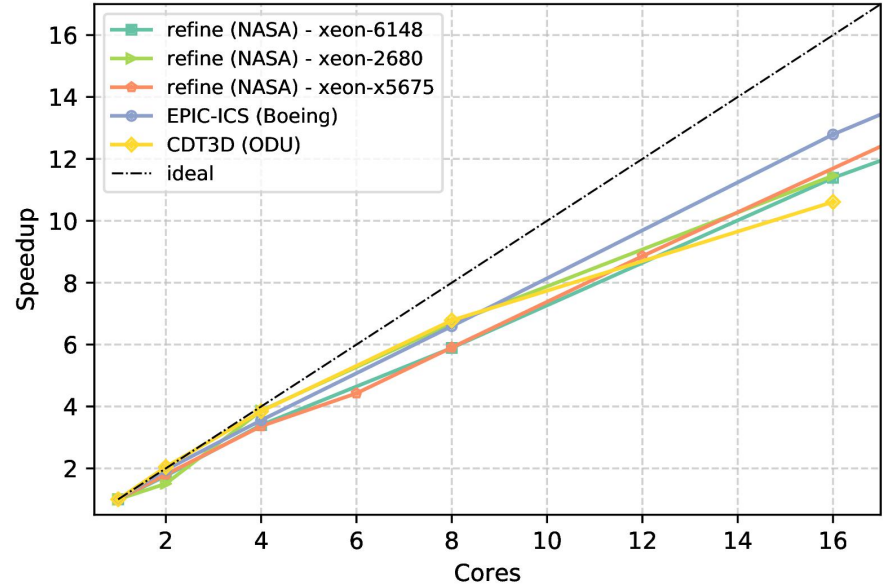
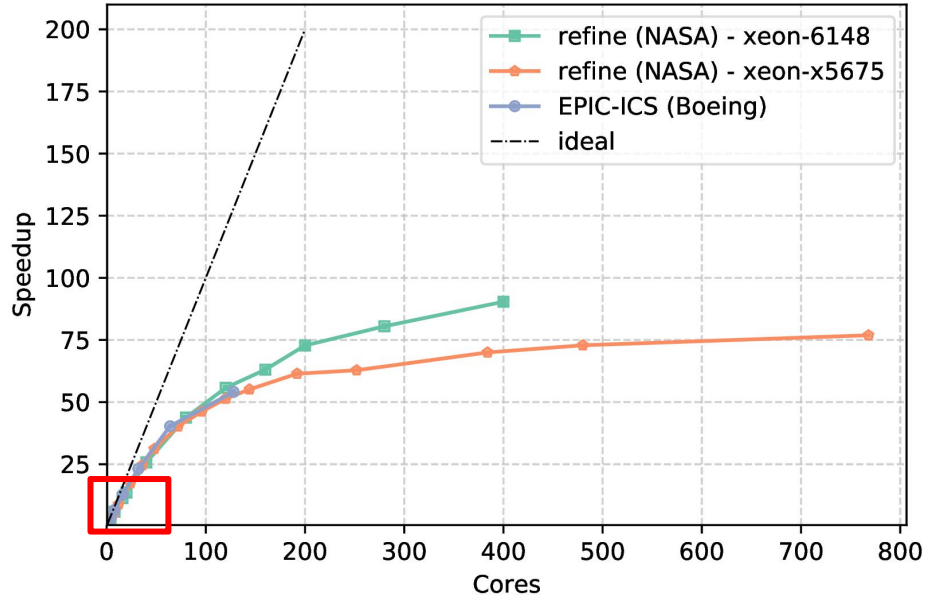
Case: Cube Polar-2



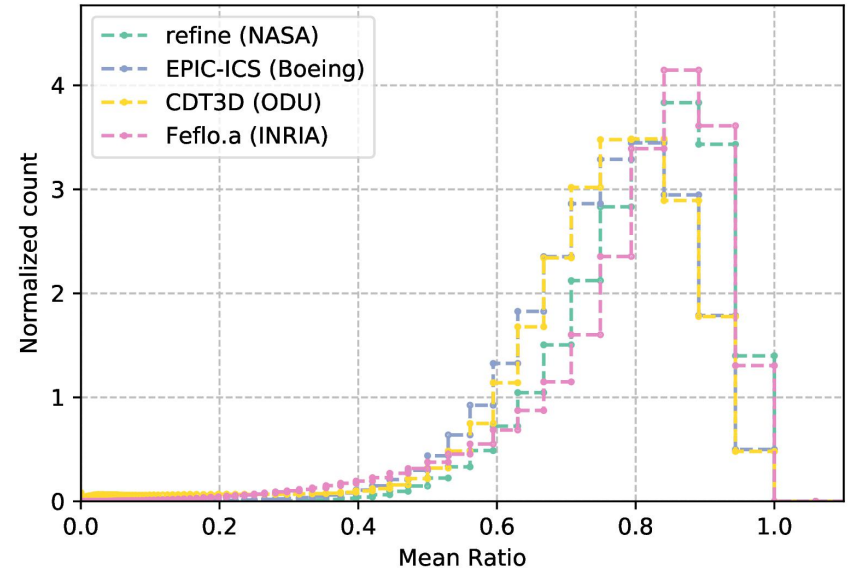
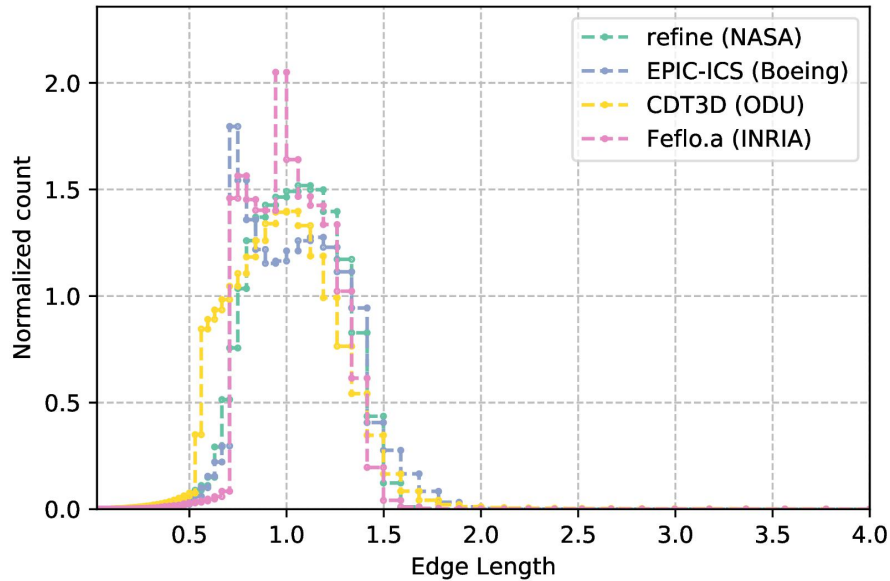
Metric tensor field :

- Analytic Metric
- Target Complexity 500k

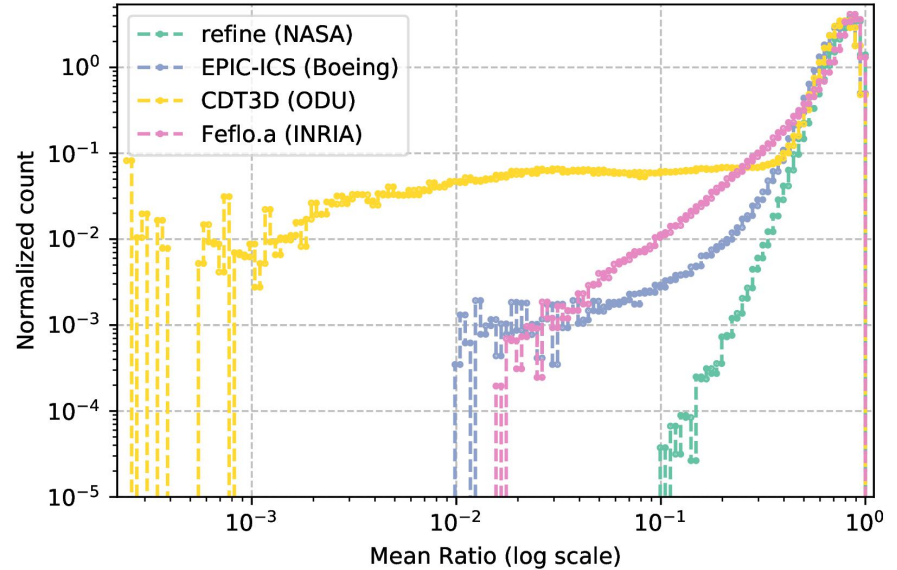
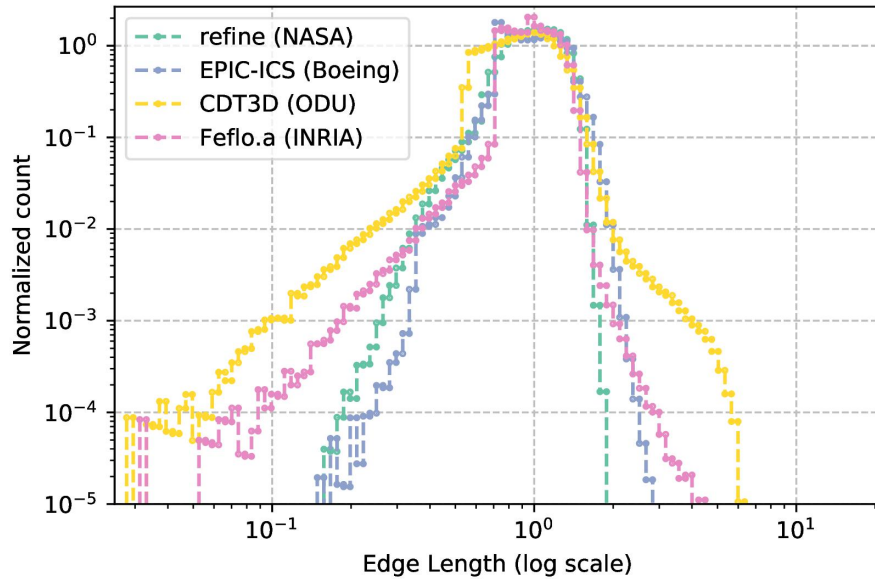
Cube Polar-2: Scalability results



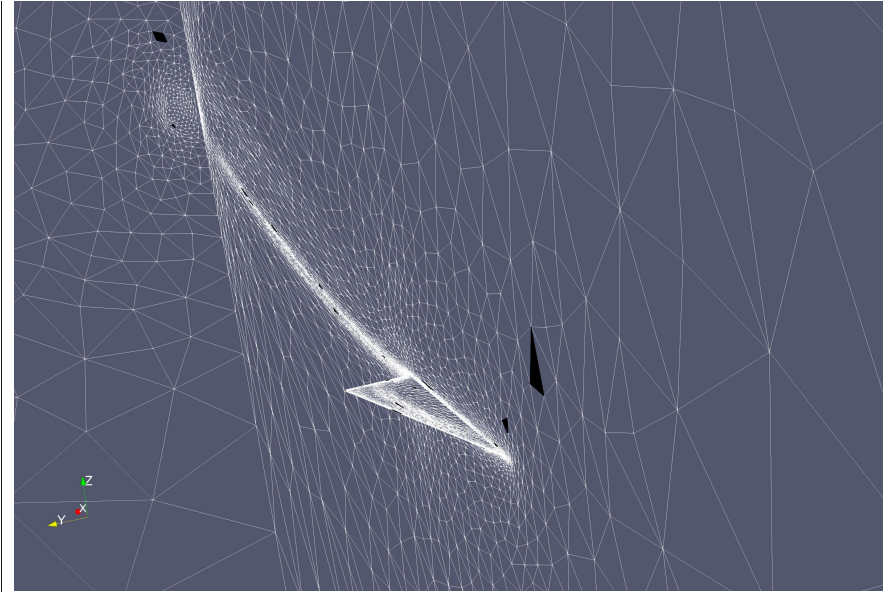
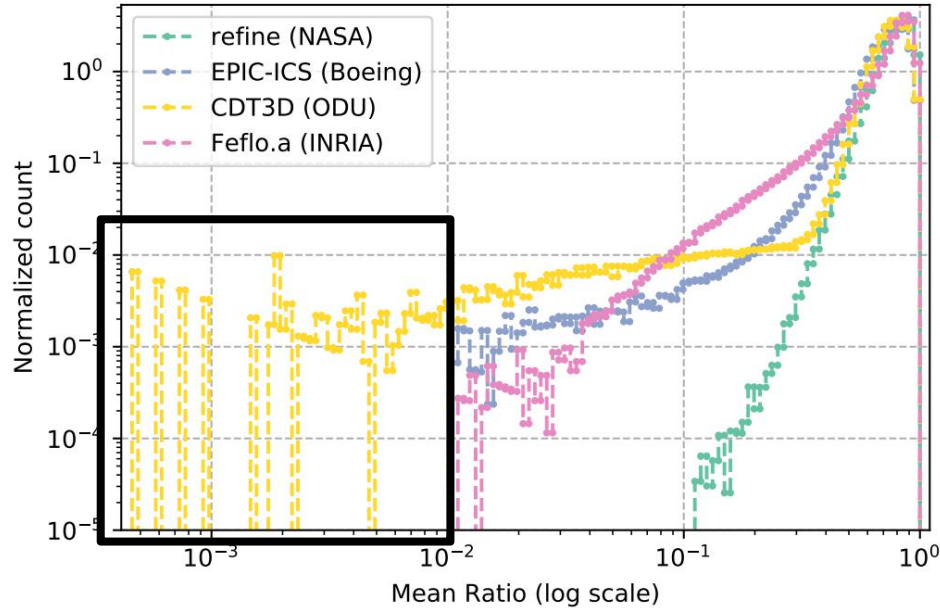
Cube Polar-2: Metric conformity results



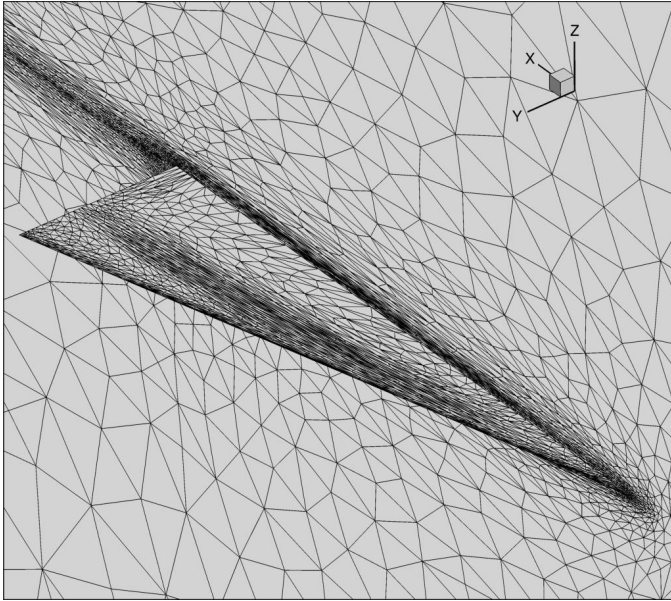
Cube Polar-2: Metric conformity results



Metric conformity results (Delta Wing)



Delta Wing Laminar Flow

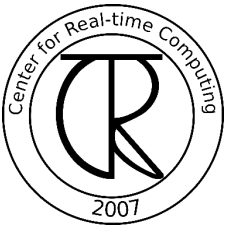


The 3D Laminar Delta Wing flow case [1]

Freestream conditions:

- 0.3 Mach,
- 4,000 Reynolds number (based on the root chord length)
- 12.5° angle of attack.

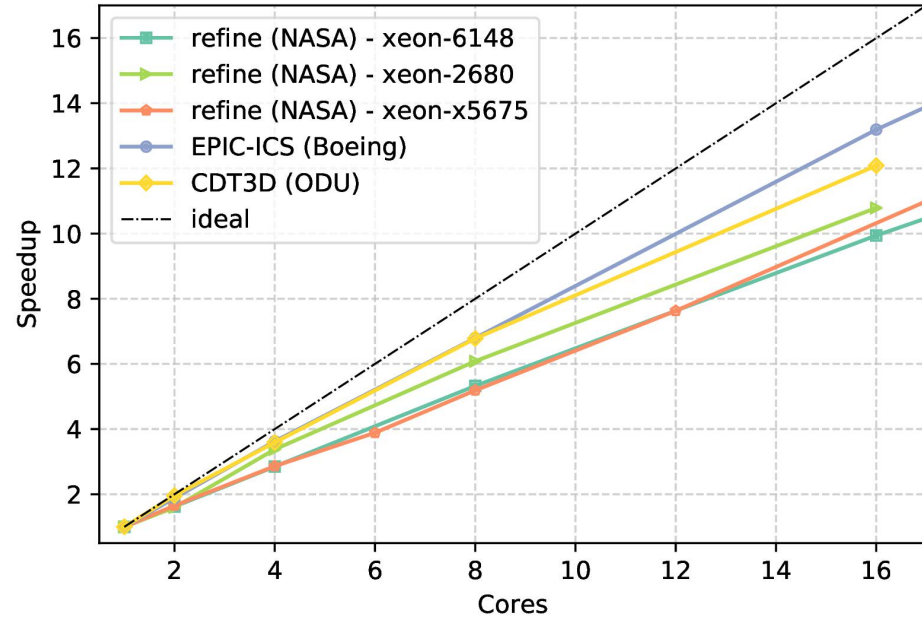
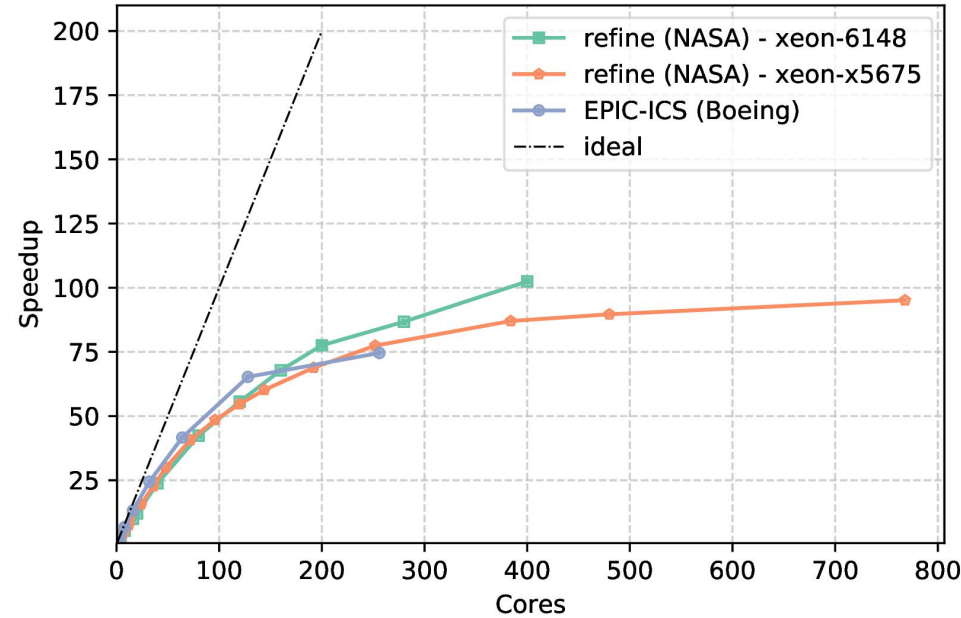
More details about the verification of the delta wing adaptation [2]



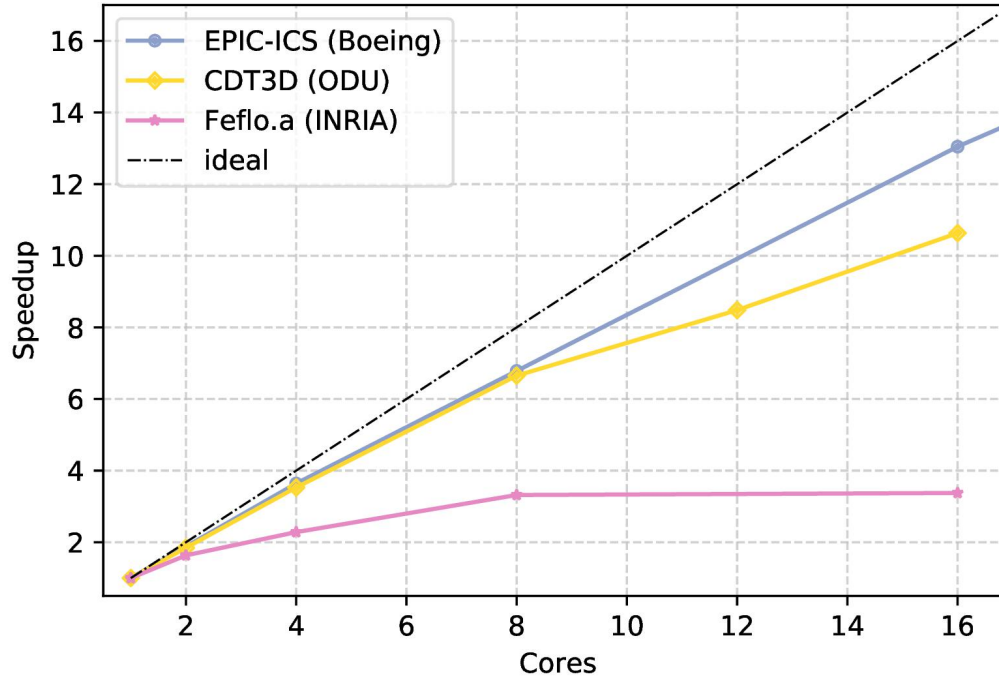
[1] Wang et al. "High-Order CFD Methods: Current Status and Perspective," International Journal for Numerical Methods in Fluids, Vol. 72, No. 8, 2013

[2] Park, M. A. et al. "Verification of Unstructured Grid Adaptation Components," AIAA SciTech Forum 2019

Delta Wing Laminar Flow *(Target complexity 500k)*



Delta Wing Laminar Flow *(Target complexity 10M)*



Delta Wing Laminar Flow (50k-> -> 12M)

Feflo.a

cores	complexity	T _{prep}	T _{e2e}	elms/sec	pts/sec
1	50k → 500k	1.9	52.0	87,65K	13,57K
3	500k → 1.5m	6.2	82.5	132,78K	20,49K
6	1.5m → 3m	23.3	111.2	138,42K	21,41K
12	3m → 6m	68.3	155.0	160,91K	24,80K
24	6m → 12m	175	223.4	183,13K	28,26K

CDT3D

cores	complexity	T _{prep}	T _{e2e}	elms/sec	pts/sec
1	50k → 500k	2.26	719.59	6,8 K	1,1K
3	500k → 1.5m	0.18	666.35	15,7K	2,6K
6	1.5m → 3m	0.48	586.14	31,1K	5,2K
12	3m → 6m	0.51	648.17	54,1K	9,0K
24	6m → 12m	0.97	859.06	81,0K	13,5K



Delta Wing Laminar Flow *(50k-→ -> 12M)*

Feflo.a

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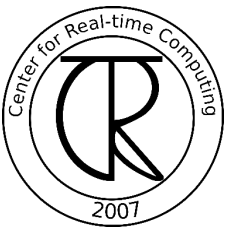
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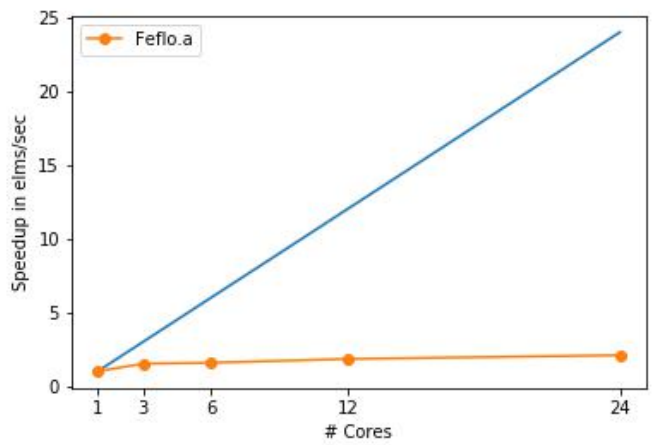
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Delta Wing Laminar Flow (50k → ... → 12M)

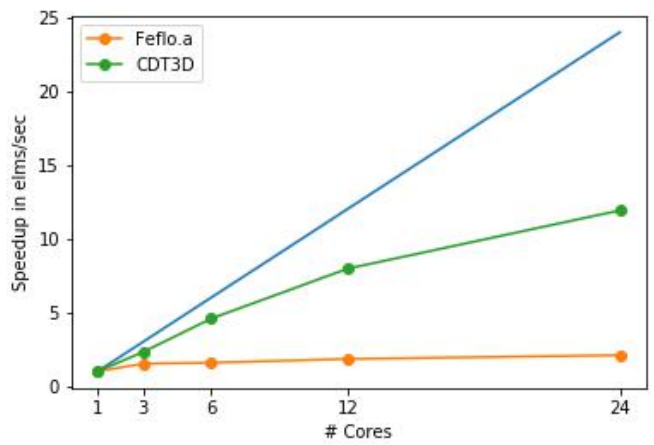
Feflo.a

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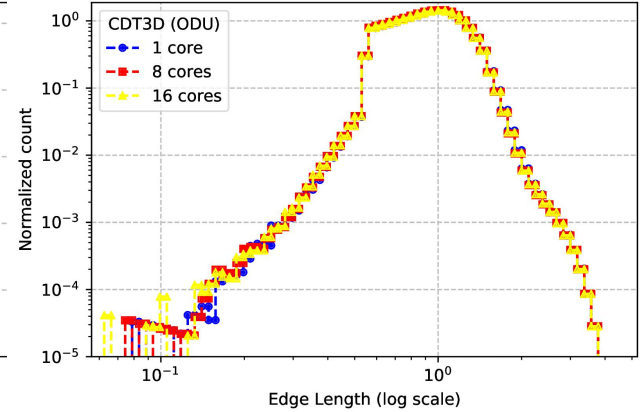
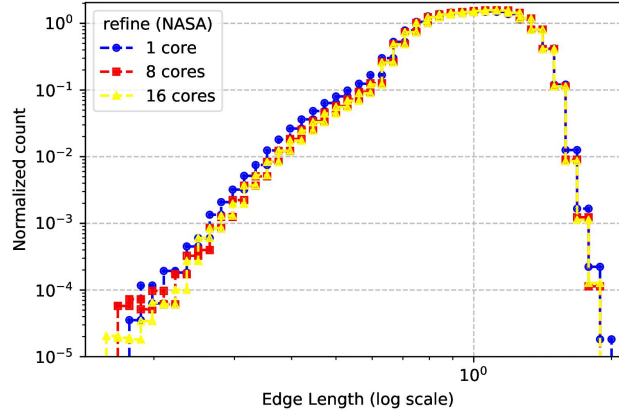
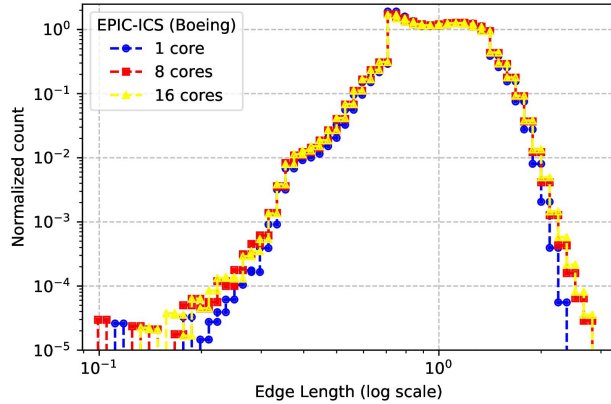


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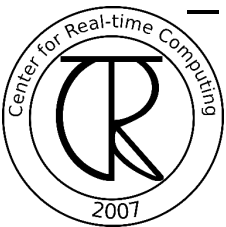
Stability



— Metric conformity is independent of number of cores

Follow-up Study

- Evaluate cases that involve balanced insertion and collapsing
 - Realistic applications utilize the full set of mesh operators
- Include curved geometries
 - Implemented through surrogate geometry or geometry kernel API
- Increase the problem size
- Include more parallel grid adaptation packages
- Educate algorithm changes to reduce execution time
 - refine now 50%-75% of the execution time reported in paper



Participate

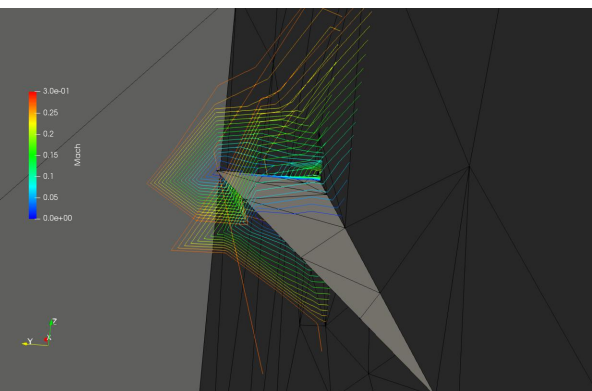
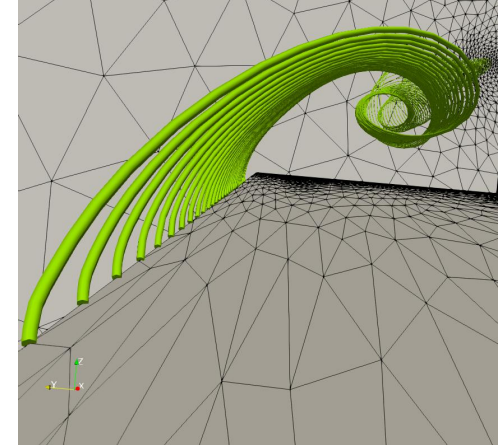
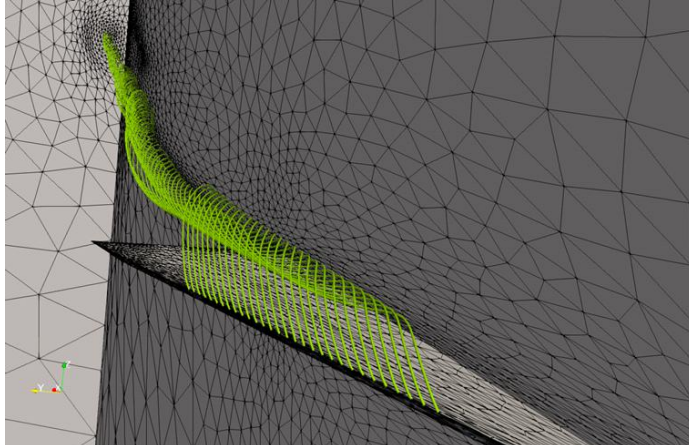
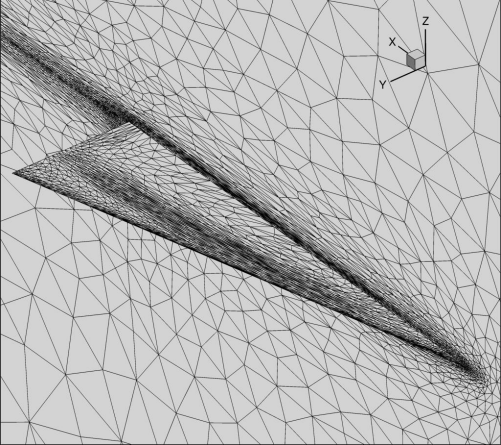
<https://ugawg.github.io/>

- Past papers & presentations

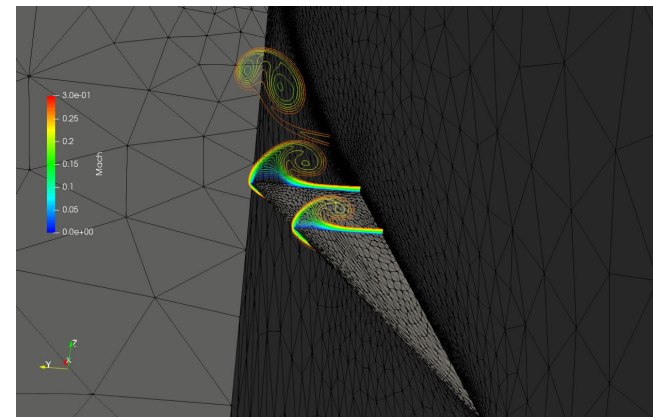
<https://github.com/UGAWG>

- Input Grids and metric fields
- Quality and speedup data





Thank you



This work is funded in part by NSF grant no. CCF-1439079, NASA grant no. NNX15AU39A, the Modeling and Simulation Fellowship at Old Dominion University and Richard T. Cheng Endowment. This work was partially supported by the Transformational Tools and Technologies (TTT) Project of the NASA Transformative Aeronautics Concepts Program (TACP)